

Satisfiability Checking

Overview

Prof. Dr. Erika Ábrahám

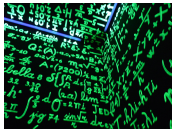
RWTH Aachen University
Informatik 2
LuFG Theory of Hybrid Systems

WS 19/20

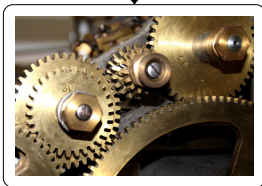
- Daniel Kroening and Ofer Strichman.
Decision Procedures: An Algorithmic Point of View.
Springer-Verlag, Berlin, 2008.
- Slides
- Selected papers
- Materials in moodle

- Language: English or German
- **Lecture (V3)**: Monday 8:30-10:00 and Tuesday 8:30-9:15, room AH III
- **Exercise (Ü1)**: Tuesday, 9:15-10:00, room AH III, after the lecture
- **Exam**: written
Mandatory online tests and programming exercise. Exercise solutions are no entrance requirement, but they are strongly recommended.
- **Assistants**:
Gereon Kremer gereon.kremer@cs.rwth-aachen.de
Rebecca Haehn haehn@cs.rwth-aachen.de

What is this lecture about?



Quantifier-free
logical
formula

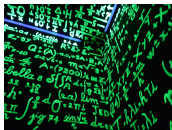


Solver

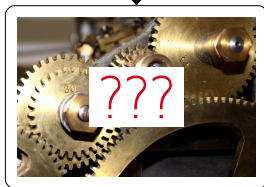


Satisfiability of the
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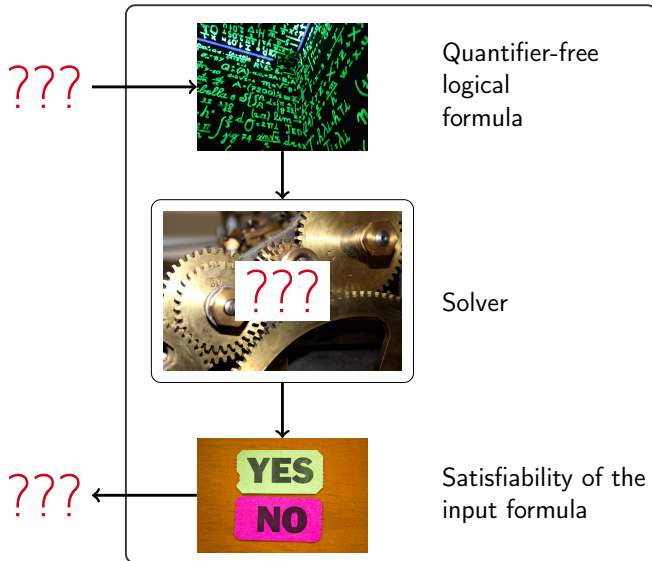


Solver



Satisfiability of the
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What is this lecture about?



The Boolean satisfiability problem...

Satisfiability problem for propositional logic

Given a **formula** combining some **atomic propositions** using the **Boolean operators** “and” ($\wedge$), “or” ($\vee$) and “not” ($\neg$), decide whether we can substitute truth values for the propositions such that the **formula evaluates to true**.

Example

Formula: $(a \vee \neg b) \wedge (\neg a \vee b \vee c)$

Satisfying assignment: $a = \text{true}, \quad b = \text{false}, \quad c = \text{true}$

It is the perhaps most well-known NP-complete problem [Cook, 1971] [Levin, 1973].

...and its extension to theories

Satisfiability modulo theories problem (informal)

Given a Boolean combination of **constraints from some theories**, decide whether we can substitute (type-correct) values for the (theory) variables such that the formula evaluates to true.

A non-linear real arithmetic example

Formula: $(x - 2y > 0 \vee x^2 - 2 = 0) \wedge x^4 y + 2x^2 - 4 > 0$

Satisfying assignment: $x = \sqrt{2}, \quad y = 2$

Hard problems... non-linear integer arithmetic is even undecidable.

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 - The logical system allows to derive the meaning of formulas.
- Important properties of logical systems:
 - consistency
 - soundness
 - completeness

Historical view on logic

Historical development goes from

informal logic (natural language arguments) to
formal logic (formal language arguments)

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- Philosophical logic
 - 500 BC to 19th century
- Symbolic logic
 - Mid to late 19th century
- Mathematical logic
 - Late 19th to mid 20th century
- Logic in computer science

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- 500 B.C - 19th century
- Logic dealing with sentences in the natural language used by humans.
- Example
 - All men are mortal.
 - Socrates is a man.
 - Therefore, Socrates is mortal.

- Natural languages are very ambiguous.
- Aristotle (384 BC – 322 BC) identified 13 types of fallacies in his *Sophistical Refutations*.



The fallacy of **composition** arises when one infers that something is true of the whole from the fact that it is true of some part of the whole.

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- 1 Human cells are invisible to the naked eye.
- 2 Humans are made up of human cells.
- 3 Therefore, humans are invisible to the naked eye.

A fallacy of **division** occurs when one reasons logically that something true of a thing must also be true of all or some of its parts.

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Famously and controversially, in the Greek philosophy it was assumed that the atoms constituting a substance must themselves have the properties of that substance: so atoms of water would be wet, atoms of iron would be hard, atoms of wool would be soft, etc.

A **figure of speech** is the use of a word or words diverging from its usual meaning.

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I had butterflies in my stomach.

Affirming the consequent is a formal fallacy, committed by reasoning in the form:

- 1 If P, then Q.
- 2 Q.
- 3 Therefore, P.

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- 1 If I have the flu, then I have a sore throat.
- 2 I have a sore throat.
- 3 Therefore, I have the flu.

Besides such fallacies, natural languages allow to argue about the language itself.

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Rules for connecting language constructs are not working the expected way:

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This sentence has five words and this sentence has five words.

→ The conjunction of two true sentences is not always true.

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Symbolic and mathematical logic

- 1854: **George Boole** introduced symbolic logic and the principles of what is now known as **Boolean logic**.
- 1879: **Gottlob Frege** created with his *Begriffsschrift* the basis of modern logic with the invention of **quantifier** notation.
- 1910-1913: **Alfred Whitehead** and **Bertrand Russell** published *Principia Mathematica* on the foundations of mathematics, attempting to derive **mathematical truths** from axioms and inference rules in symbolic logic.
- 1931: **Gödel**'s and **Turing**'s **undecidability results** (we will deal with them later).



George Boole
(1815-1864)



Gottlob Frege
(1848-1925)

Symbolic and mathematical logic

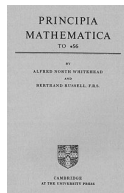
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Bertrand Russell
(1872-1970)



Alfred Whitehead
(1861-1947)



*54·43. $\vdash \therefore \alpha, \beta \in 1 . \supset : \alpha \cap \beta = \Lambda . \equiv . \alpha \cup \beta \in 2$

Dem.

$\vdash . *54·26 . \supset \vdash \therefore \alpha = t'x . \beta = t'y . \supset : \alpha \cup \beta \in 2 . \equiv . x \neq y .$

[*51·231] $\equiv . t'x \cap t'y = \Lambda .$

[*13·12] $\equiv . \alpha \cap \beta = \Lambda \quad (1)$

$\vdash . (1) . *11·11·35 . \supset$

$\vdash \therefore (\exists x, y) . \alpha = t'x . \beta = t'y . \supset : \alpha \cup \beta \in 2 . \equiv . \alpha \cap \beta = \Lambda \quad (2)$

$\vdash . (2) . *11·54 . *52·1 . \supset \vdash . \text{Prop}$

From this proposition it will follow, when arithmetical addition has been defined, that $1 + 1 = 2$.

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Kurt Gödel
(1906-1978)



Alan Turing
(1912-1954)

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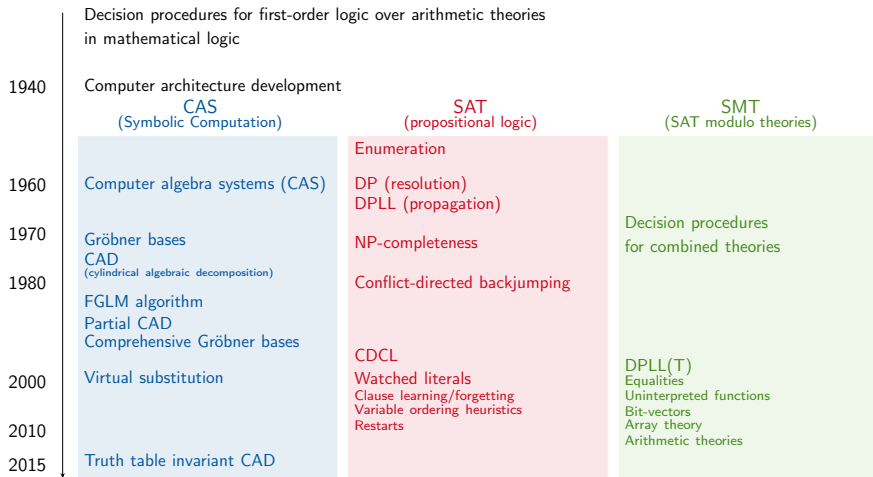
Logic has a profound impact on **computer science**. Some examples:

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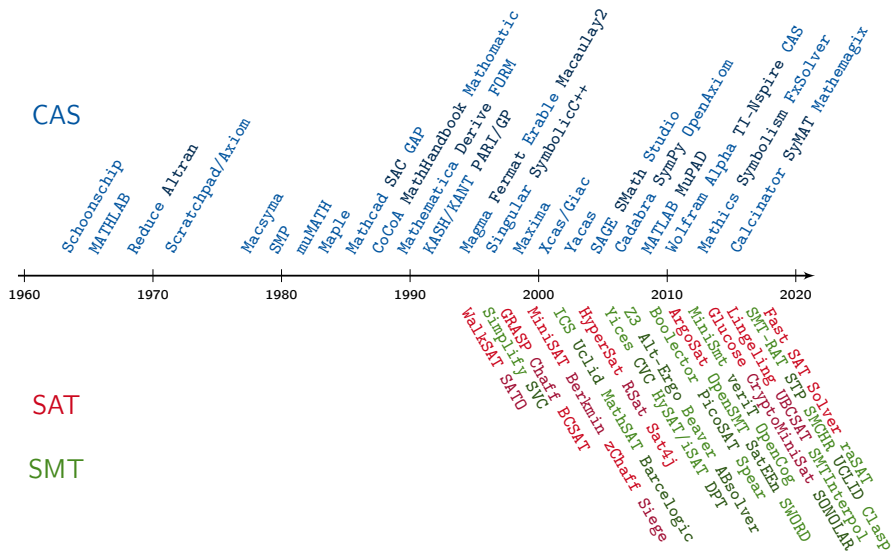
- Propositional logic - the foundation of computers and circuits
- Databases - Query languages
- Programming languages (e.g. Prolog)
- Specification and verification
- ...

- Propositional logic
- First order logic
- Higher order logic
- Temporal logic
- ...

Satisfiability checking: Some milestones



Satisfiability checking: Tool development (not exhaustive)



Satisfiability checking for propositional logic

Success story: SAT-solving

- Practical problems with millions of variables are solvable.
- Frequently used in different research areas for, e.g., analysis, synthesis and optimisation.
- Also massively used in industry for, e.g., digital circuit design and verification.

Satisfiability checking for propositional logic

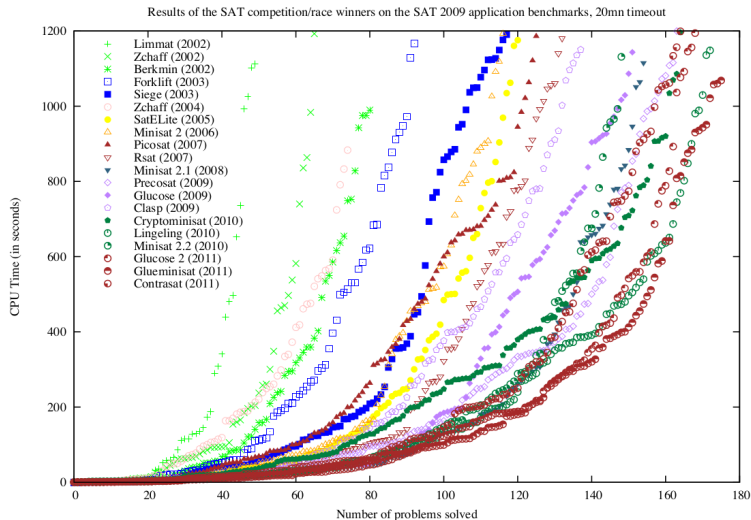
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Community support:

- Standardised input language, lots of benchmarks available.
- Competitions since 2002.
2016 SAT Competition: 6 tracks, 29 solvers in the main track.
SAT Live! forum as community platform, dedicated conferences, journals, etc.

An impression of the SAT solver development



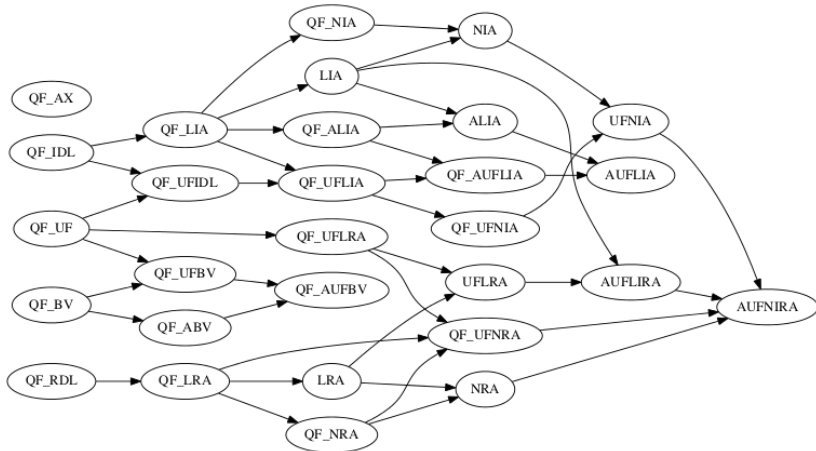
Source: Jarvisalo, Le Berre, Roussel, Simon. *The International SAT Solver Competitions*. AI Magazine, 2012.

Satisfiability modulo theories solving

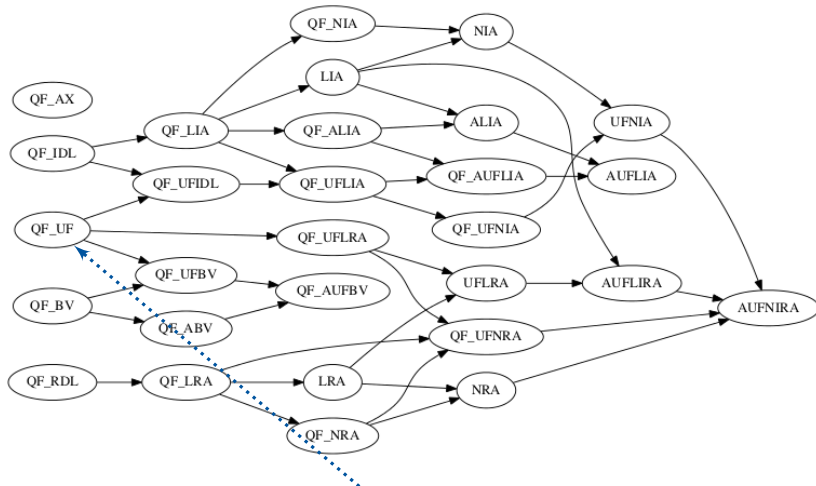
- Propositional logic is sometimes too weak for modelling.
- We need more expressive **logics** and **decision procedures** for them.
- Logics:
 - quantifier-free fragments of first-order logic over various theories.
- Our focus: SAT-modulo-theories (SMT) solving.

- Propositional logic is sometimes too weak for modelling.
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- Our focus: **SAT-modulo-theories (SMT) solving**.
- **SMT-LIB as standard input language** since 2004.
- **Competitions** since 2005.
- **SMT-COMP 2016** competition:
 - 4 tracks, 41 logical categories.
 - **QF linear real arithmetic**: 7 + 2 solvers, 1626 benchmarks.
 - **QF linear integer arithmetic**: 6 + 2 solvers, 5839 benchmarks.
 - **QF non-linear real arithmetic**: 5 + 1 solvers, 10245 benchmarks.
 - **QF non-linear integer arithmetic**: 7 + 1 solvers, 8593 benchmarks.

SMT-LIB theories

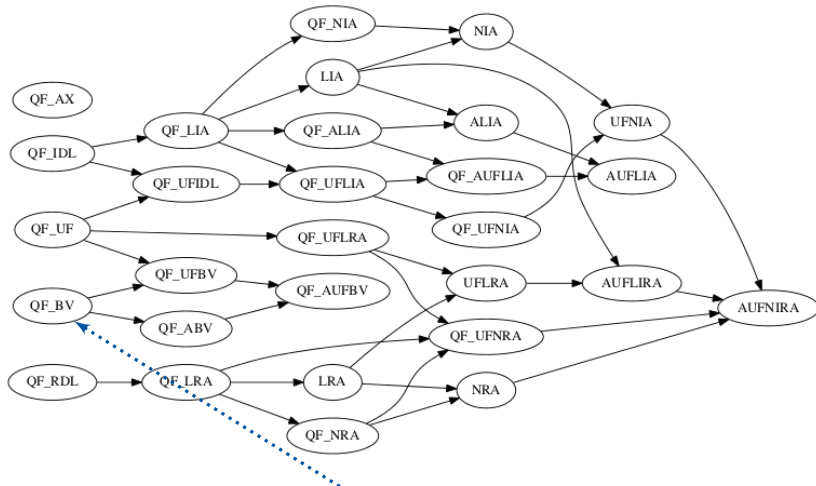


Source: <http://smtlib.cs.uiowa.edu/logics.shtml>



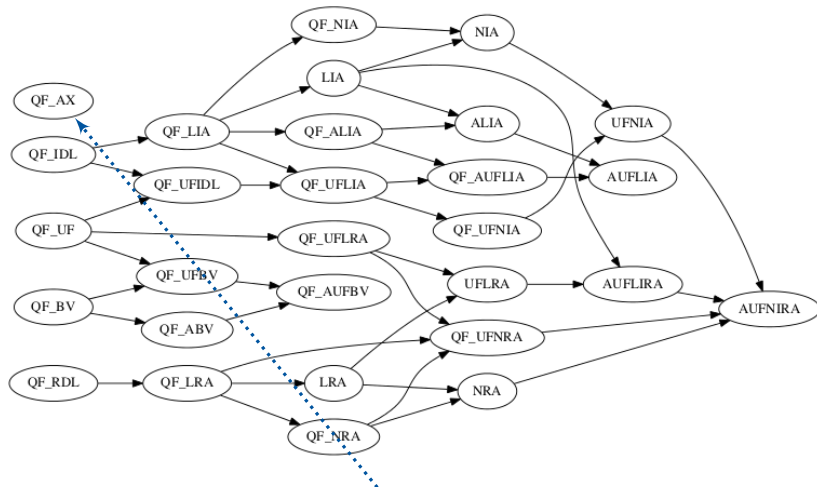
Quantifier-free equality logic with uninterpreted functions
 $(a = c \wedge b = d) \rightarrow f(a, b) = f(c, d)$

SMT-LIB theories



Source: <http://smtlib.cs.uiowa.edu/logics.shtml>

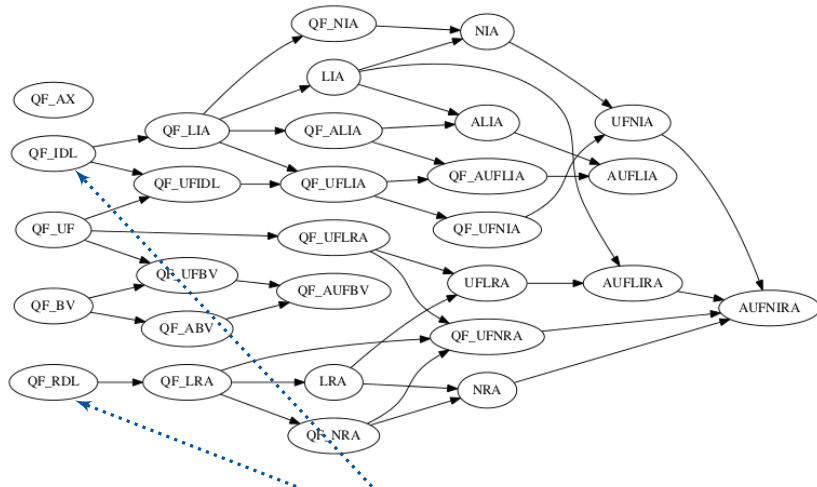
SMT-LIB theories



Quantifier-free array theory
 $i = j \rightarrow \text{read}(\text{write}(a, i, v), j) = v$

Source: <http://smtlib.cs.uiowa.edu/logics.shtml>

SMT-LIB theories

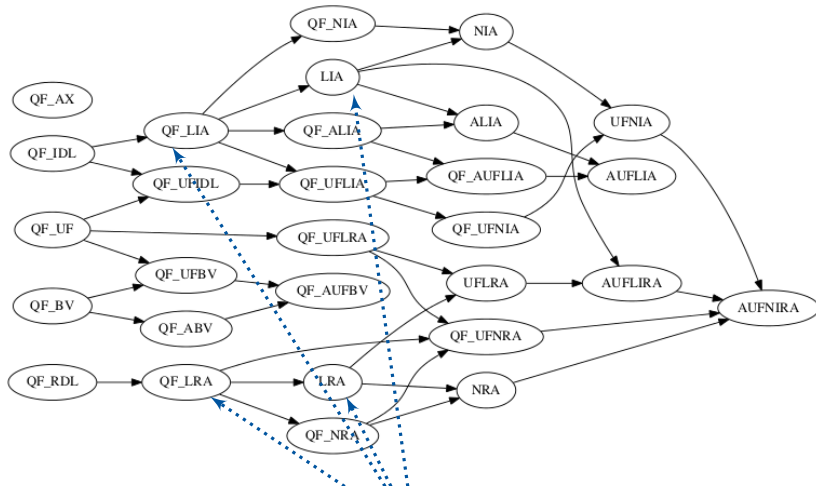


Quantifier-free integer/rational difference logic

$$x - y \geq 0 \vee x - z < 0$$

Source: <http://smtlib.cs.uiowa.edu/logics.shtml>

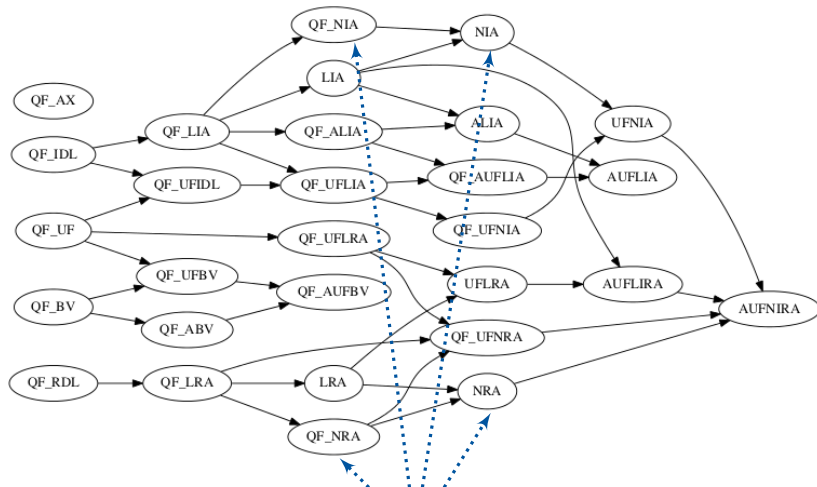
SMT-LIB theories



(Quantifier-free) real/integer linear arithmetic
 $4x + 7y = 8 \wedge (y = 0 \vee x > y)$

Source: <http://smtlib.cs.uiowa.edu/logics.shtml>

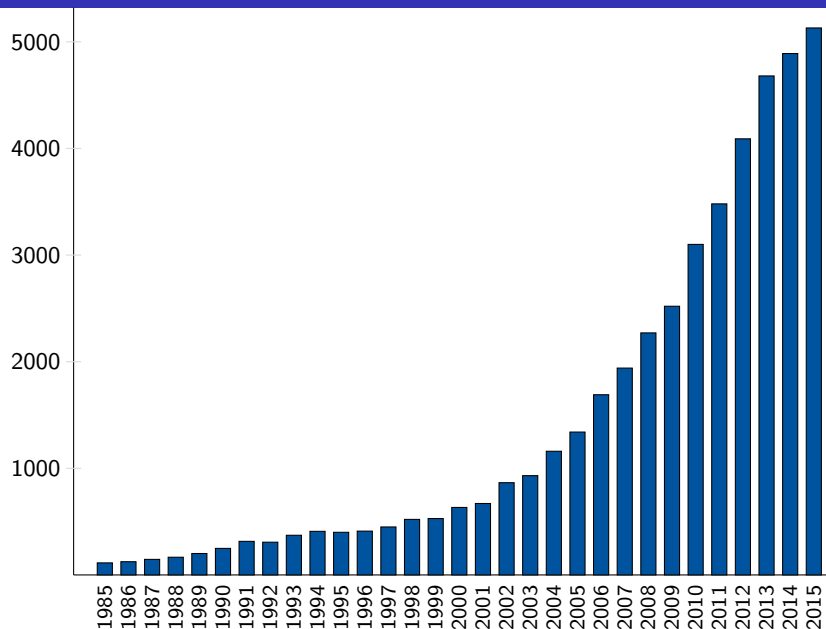
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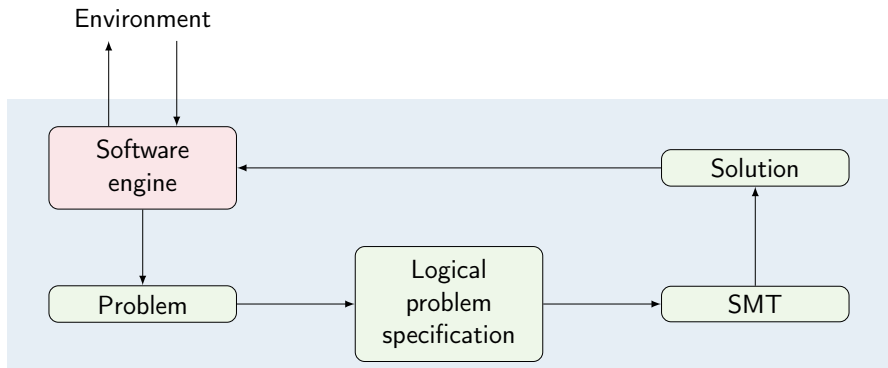
(Quantifier-free) real/integer non-linear arithmetic
 $x^2 + 2xy + y^2 > 0 \vee (x \geq 1 \wedge xz + yz^2 = 0)$

Source: <http://smtlib.cs.uiowa.edu/logics.shtml>

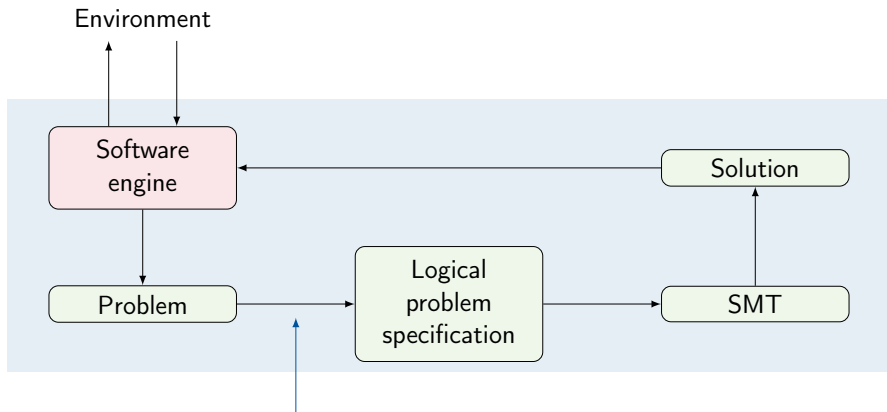
Google Scholar search for “SAT modulo theories”



SAT/SMT embedding structure

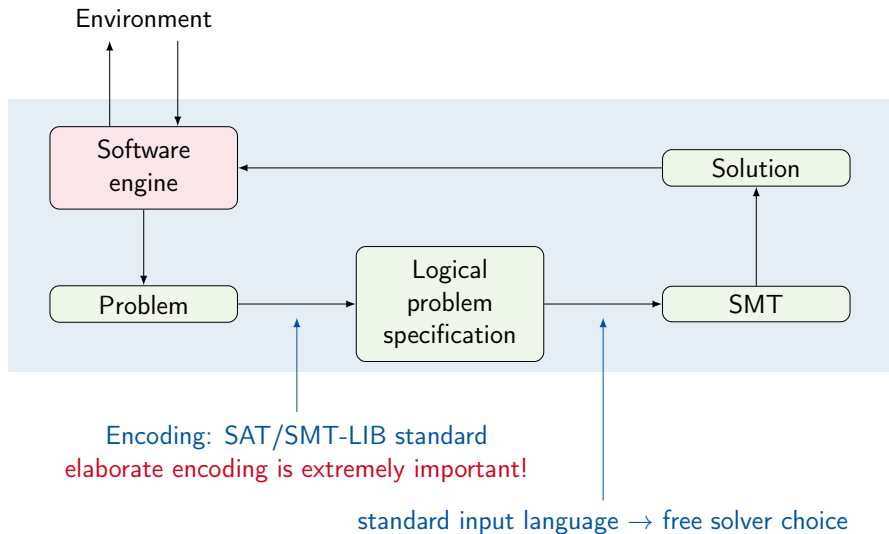


SAT/SMT embedding structure



Encoding: SAT/SMT-LIB standard
elaborate encoding is extremely important!

SAT/SMT embedding structure



Application example: Hardware verification

Problem 1: Given two circuits, are they equivalent?

Problem 2: Given a circuit and a property specification, does the circuit fulfill the specification?

Problem 3: Given a partially specified circuit with a black-box component (at early design stage) and a property specification, is the partial circuit realisable, i.e., is there an implementation of the black box such that the circuit fulfills the property?

Many hardware producers develop and use own SAT solvers for these tasks.

Application example: Symbolic execution

Program 1.2.1 A recursion-free program with bounded loops and an SSA unfolding.

```
int Main(int x, int y)
{
    if (x < y)
        x = x + y;
    for (int i = 0; i < 3; ++i) {
        y = x + Next(y);
    }
    return x + y;
}

int Next(int x) {
    return x + 1;
}
```

```
int Main(int x0, int y0)
{
    int x1;
    if (x0 < y0)
        x1 = x0 + y0;
    else
        x1 = x0;
    int y1 = x1 + y0 + 1;
    int y2 = x1 + y1 + 1;
    int y3 = x1 + y2 + 1;
    return x1 + y3;
}
```

$$\exists x_1, y_1, y_2, y_3 \left((x_0 < y_0 \implies x_1 = x_0 + y_0) \wedge (\neg(x_0 < y_0) \implies x_1 = x_0) \wedge \right. \\ \left. y_1 = x_1 + y_0 + 1 \wedge y_2 = x_1 + y_1 + 1 \wedge y_3 = x_1 + y_2 + 1 \wedge \right. \\ \left. result = x_1 + y_3 \right)$$

Source: Nikolaj Bjørner and Leonardo de Moura. *Applications of SMT solvers to Program Verification*.

Rough notes for SSFT 2014.

Application example: Bounded model checking

Problem: Given a program (automaton, circuit, term rewrite system, etc.), find an execution path of length at most k which leads to a state with a certain property (used for detecting, e.g., division by zero, violating functional requirements, etc.).

Application example: Bounded model checking for C/C++



**Bounded Model Checking
for Software**



CBMC About CBMC

CBMC is a Bounded Model Checker for C and C++ programs. It supports C89, C99, most of C11 and most compiler extensions provided by gcc and Visual Studio. It also supports [SystemC](#) using [Scoot](#). We have recently added experimental support for Java Bytecode.

CBMC verifies array bounds (buffer overflows), pointer safety, exceptions and user-specified assertions. Furthermore, it can check C and C++ for consistency with other languages, such as Verilog. The verification is performed by unwinding the loops in the program and passing the resulting equation to a decision procedure.



While CBMC is aimed for embedded software, it also supports dynamic memory allocation using `malloc` and `new`. For questions about CBMC, contact [Daniel Kroening](#).

CBMC is available for most flavours of Linux (pre-packaged on Debian, Ubuntu and Fedora), Solaris 11, Windows and MacOS X. You should also read the [CBMC license](#).

CBMC comes with a built-in solver for bit-vector formulas that is based on MiniSat. As an alternative, CBMC has featured support for external SMT solvers since version 3.3. The solvers we recommend are (in no particular order) [Boolector](#), [MathSAT](#), [Yices 2](#) and [Z3](#). Note that these solvers need to be installed separately and have different licensing conditions.

Source: D. Kroening. **CBMC home page**. <http://www.cprover.org/cbmc/>

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Logical encoding of finite unsafe paths

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Encoding idea: $Init(s_0) \wedge Trans(s_0, s_1) \wedge \dots \wedge Trans(s_{k-1}, s_k) \wedge Bad(s_0, \dots, s_k)$

tions and user-specified assertions. Furthermore, it can check C and C++ for consistency with other languages, such as Verilog. The verification is performed by unwinding the loops in the program and passing the resulting equation to a decision procedure.



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Logical encoding of finite unsafe paths

CBMC is a Bounded Model Checker for C and C++ programs. It supports C89, C99, most of C11 and most compiler extensions provided by gcc and Visual Studio. It also supports [SystemC](#) using [Scoot](#). We have recently added experimental support for Java [Bytecode](#).



Encoding idea: $Init(s_0) \wedge Trans(s_0, s_1) \wedge \dots \wedge Trans(s_{k-1}, s_k) \wedge Bad(s_0, \dots, s_k)$

tions and user-specified assertions. Furthermore, it can check C and C++ for consistency with other languages, such as Verilog. The verification passing the

While CBMC using mal

CBMC is a Solaris 11.

CBMC co alternative

solvers we recommend are (in no particular order) [Boolector](#), [MathSAT](#), [ices 2](#) and [ices 3](#). Note that these solvers need to be installed separately and have different licensing conditions.

Application examples:
Error localisation and explanation
Equivalence checking
Test case generation
Worst-case execution time

location

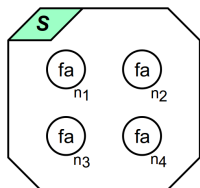
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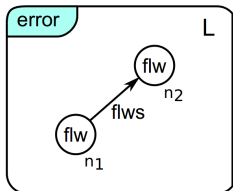
3. The

Source: D. Kroening. **CBMC home page**. <http://www.cprover.org/cbmc/>

Application example: BMC for graph transformation systems



(a) Initial graph S



(b) Forbidden pattern

Fig. 1. Part of the car platooning GTS [11]

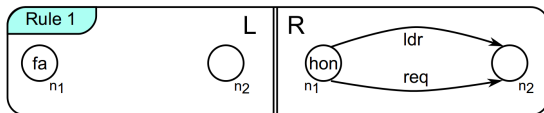


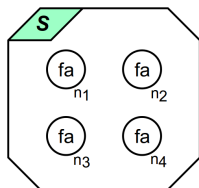
Fig. 2. Rule 1 of the car platooning GTS [11]

Source: T. Isenberg, D. Steenken, and H. Wehrheim.

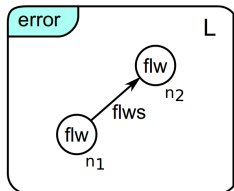
Bounded Model Checking of Graph Transformation Systems via SMT Solving.

In Proc. FMOODS/FORTE'13.

Application example: BMC for graph transformation systems



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Fig. 1. Part of the car platooning GTS [11]

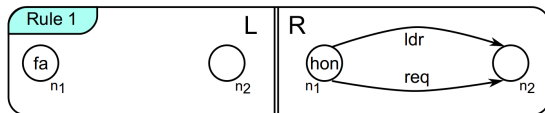


Fig. 2. Rule 1 of the car platooning GTS [11]

Encode initial and forbidden state graphs and the graph transformation rules in first-order logic.



Apply bounded model checking

Source: T. Isenberg, D. Steenken, and H. Wehrheim.

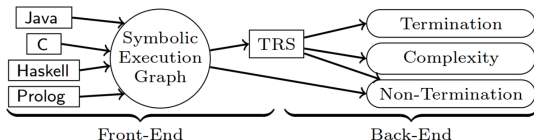
Bounded Model Checking of Graph Transformation Systems via SMT Solving.

In Proc. FMOODS/FORTE'13.

Application example: Termination analysis for programs

AProVE

Automated Program Verification Environment



Source: T. Ströder, C. Aschermann, F. Frohn, J. Hensel, J. Giesl.

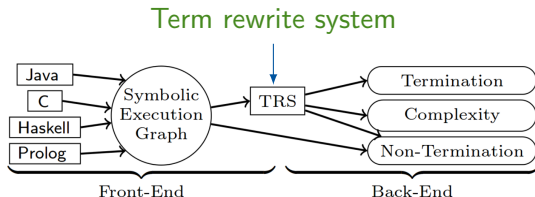
AProVE: Termination and memory safety of C programs (competition contribution).

In Proc. TACAS'15.

Application example: Termination analysis for programs

AProVE

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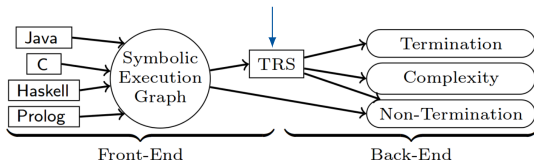
In Proc. TACAS'15.

Application example: Termination analysis for programs

APROVE

Automated Program Verification Environment

Term rewrite system



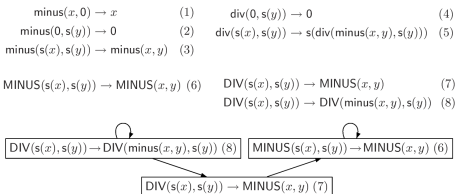
Term rewrite system



Dependency pairs



Chains



Logical encoding for well-founded orders.

Source: T. Ströder, C. Aschermann, F. Frohn, J. Hensel, J. Giesl.

AProVE: Termination and memory safety of C programs (competition contribution).

In Proc. TACAS'15.

Application example: jUnit_{RV} for runtime verification of multi-threaded, object-oriented systems

Properties: linear temporal logics enriched with first-order theories

Method: SMT solving + classical monitoring

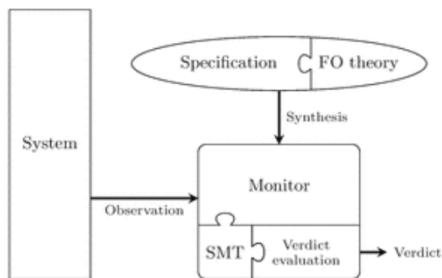


Fig. 1 Schematic overview of the monitoring approach

Source: N. Decker, M. Leucker, D. Thoma.

Monitoring modulo theories.

International Journal on Software Tools for Technology Transfer, 18(2):205-225, April 2016.

Application example: Planning

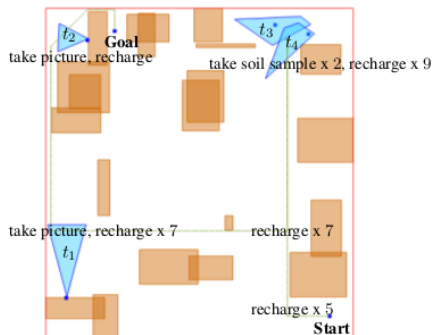


Figure 1: A GEOMETRIC ROVERS example instance, showing the starting and goal locations of the rover, areas where tasks can be performed (blue) and obstacles (orange) and a plan solving the task (green). The red box indicates the bounds of the environment.

Source: E. Scala, M. Ramirez, P. Haslum, S. Thiebaux.

Numeric planning with disjunctive global constraints via SMT.

In Proc. of ICASP'16.

Application example: Scheduling

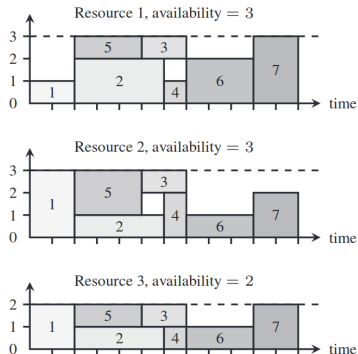
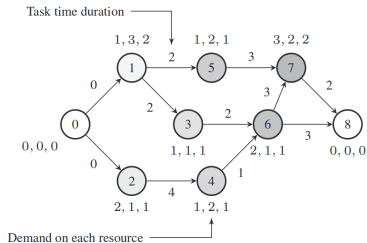


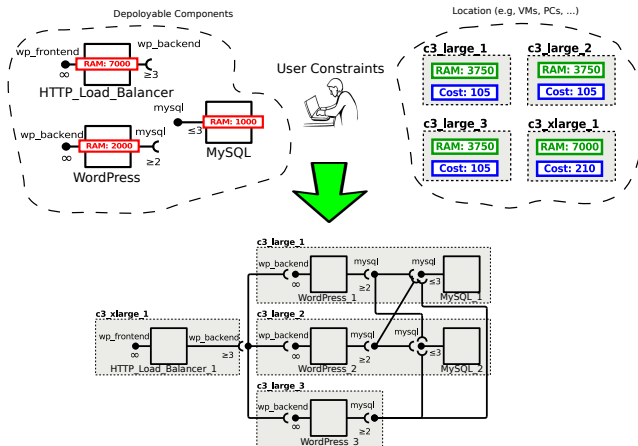
Figure 1: An example of RCPSP (Liess and Michelon 2008)

Source: C. Ansótegui, M. Bofill, M. Palahí, J. Suy, M. Villaret.

Satisfiability modulo theories: An efficient approach for the resource-constrained project scheduling problem.

Proc. of SARA'11.

Application example: Deployment optimisation on the cloud

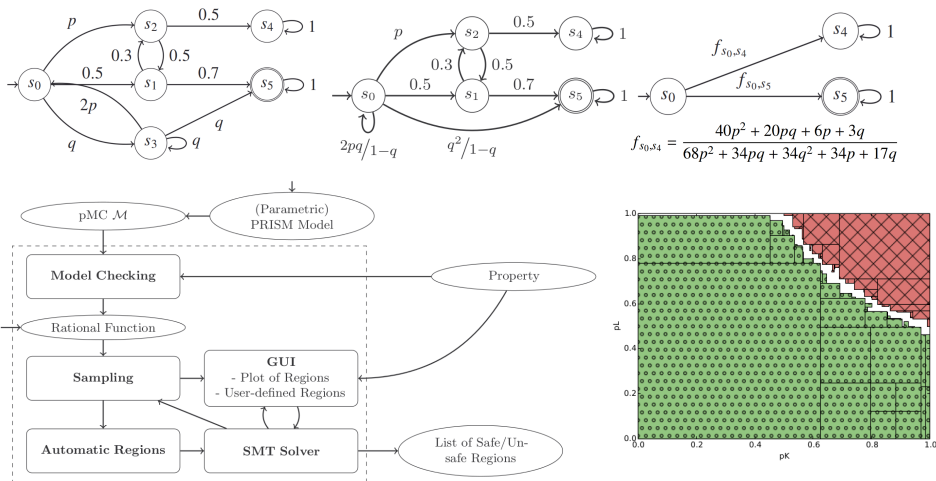


Source: E. Ábrahám, F. Corzilius, E. Broch Johnsen, G. Kremer, J. Mauro.

Zephyrus2: On the fly deployment optimization using SMT and CP technologies.

Submitted to SETTA'16.

Application example: Parameter synthesis for probabilistic systems



Source: C. Dehnert, S. Junges, N. Jansen, F. Corzilius, M. Volk, H. Brientjes, J.-P. Katoen, E. Ábrahám.

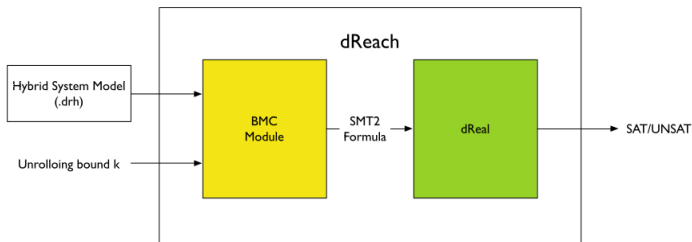
Application example: Hybrid systems reachability analysis



DREAL DREACH BENCHMARKS PUBLICATION DOWNLOAD TRY ONLINE PEOPLE

dReach is a tool for safety verification of hybrid systems.

It answers questions of the type: Can a hybrid system run into an unsafe region of its state space? This question can be encoded to SMT formulas, and answered by our SMT solver. **dReach** is able to handle general hybrid systems with nonlinear differential equations and complex discrete mode-changes.



Source: D. Bryce, J. Sun, P. Zuliani, Q. Wang, S. Gao, F. Shmarov, S. Kong, W. Chen, Z. Tavares. **dReach home page**. <http://dreal.github.io/dReach/>